

Friday 18 May 2012 – Morning

AS GCE MATHEMATICS (MEI)

4755 Further Concepts for Advanced Mathematics (FP1)

QUESTION PAPER

Candidates answer on the Printed Answer Book.

OCR supplied materials:

- Printed Answer Book 4755
- MEI Examination Formulae and Tables (MF2)

Other materials required:

- Scientific or graphical calculator

Duration: 1 hour 30 minutes



INSTRUCTIONS TO CANDIDATES

These instructions are the same on the Printed Answer Book and the Question Paper.

- The Question Paper will be found in the centre of the Printed Answer Book.
- Write your name, centre number and candidate number in the spaces provided on the Printed Answer Book. Please write clearly and in capital letters.
- **Write your answer to each question in the space provided in the Printed Answer Book.** Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Use black ink. HB pencil may be used for graphs and diagrams only.
- Read each question carefully. Make sure you know what you have to do before starting your answer.
- Answer **all** the questions.
- Do **not** write in the bar codes.
- You are permitted to use a scientific or graphical calculator in this paper.
- Final answers should be given to a degree of accuracy appropriate to the context.

INFORMATION FOR CANDIDATES

This information is the same on the Printed Answer Book and the Question Paper.

- The number of marks is given in brackets [] at the end of each question or part question on the Question Paper.
- You are advised that an answer may receive **no marks** unless you show sufficient detail of the working to indicate that a correct method is being used.
- The total number of marks for this paper is **72**.
- The Printed Answer Book consists of **16** pages. The Question Paper consists of **4** pages. Any blank pages are indicated.

INSTRUCTION TO EXAMS OFFICER/INVIGILATOR

- Do not send this Question Paper for marking; it should be retained in the centre or recycled. Please contact OCR Copyright should you wish to re-use this document.

Section A (36 marks)

- 1 You are given that the matrix $\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$ represents a transformation A, and that the matrix $\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$ represents a transformation B.
- (i) Describe the transformations A and B. [2]
- (ii) Find the matrix representing the composite transformation consisting of A followed by B. [2]
- (iii) What single transformation is represented by this matrix? [1]
- 2 You are given that z_1 and z_2 are complex numbers.
 $z_1 = 3 + 3\sqrt{3}j$, and z_2 has modulus 5 and argument $\frac{\pi}{3}$.
- (i) Find the modulus and argument of z_1 , giving your answers exactly. [4]
- (ii) Express z_2 in the form $a + bj$, where a and b are to be given exactly. [2]
- (iii) Explain why, when plotted on an Argand diagram, z_1 , z_2 and the origin lie on a straight line. [1]
- 3 The cubic equation $3x^3 + 8x^2 + px + q = 0$ has roots α , $\frac{\alpha}{6}$ and $\alpha - 7$. Find the values of α , p and q . [6]
- 4 Solve the inequality $\frac{3}{x-4} > 1$. [4]
- 5 (i) Show that $\frac{1}{2r+1} - \frac{1}{2r+3} \equiv \frac{2}{(2r+1)(2r+3)}$. [2]
- (ii) Use the method of differences to find $\sum_{r=1}^{30} \frac{1}{(2r+1)(2r+3)}$, expressing your answer as a fraction. [5]
- 6 A sequence is defined by $a_1 = 1$ and $a_{k+1} = 3(a_k + 1)$.
- (i) Calculate the value of the third term, a_3 . [1]
- (ii) Prove by induction that $a_n = \frac{5 \times 3^{n-1} - 3}{2}$. [6]

Section B (36 marks)

- 7 A curve has equation $y = \frac{x^2 - 25}{(x - 3)(x + 4)(3x + 2)}$.
- (i) Write down the coordinates of the points where the curve crosses the axes. [3]
- (ii) Write down the equations of the asymptotes. [4]
- (iii) Determine how the curve approaches the horizontal asymptote for large positive values of x , and for large negative values of x . [3]
- (iv) Sketch the curve. [4]
- 8 (i) Verify that $1 + 3j$ is a root of the equation $3z^3 - 2z^2 + 22z + 40 = 0$, showing your working. [4]
- (ii) Explain why the equation must have exactly one real root. [1]
- (iii) Find the other roots of the equation. [5]
- 9 You are given that $\mathbf{A} = \begin{pmatrix} -3 & -4 & 1 \\ 2 & 1 & k \\ 7 & -1 & -1 \end{pmatrix}$, $\mathbf{B} = \begin{pmatrix} -4 & -5 & 11 \\ -19 & -4 & -7 \\ -9 & -31 & 2 - k \end{pmatrix}$ and
- $$\mathbf{AB} = \begin{pmatrix} 79 & 0 & -3 - k \\ -9k - 27 & -31k - 14 & q \\ p & 0 & 82 + k \end{pmatrix}$$
- where
- p
- and
- q
- are to be determined.
- (i) Show that $p = 0$ and $q = 15 + 2k - k^2$. [3]
- It is now given that $k = -3$.
- (ii) Find \mathbf{AB} and hence write down the inverse matrix \mathbf{A}^{-1} . [5]
- (iii) Use a matrix method to find the values of x , y and z that satisfy the equation $\mathbf{A} \begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} 14 \\ -23 \\ 9 \end{pmatrix}$. [4]

THERE ARE NO QUESTIONS WRITTEN ON THIS PAGE



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